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Name of the Department	:	Physics
Name of the Course	:	B. Sc. (H) Physics – CBCS – NC
Semester	:	I
Name of the Paper	:	Mathematical Physics I
Unique Paper Code	:	32221101
Question Paper Set Number	:	A
Maximum Marks	:	75

### Instruction for Candidates

1. Attempt **FOUR** questions in all.
2. All questions carry equal marks.

#### 1. Solve the following first order differential equations

- a.  $(2x + 3y)dx + (y - x)dy = 0$
- b.  $(x - 2)\frac{dy}{dx} = y + 2(x - 2)^3$
- c.  $(x^2 + y^2)dy - xy dx = 0$
- d. A machine produces 1% defective components. If the random variable X is the number of defective components in production of 50 components, then find the probabilities that X takes the value 2.

#### 2. Solve the following second order differential equations

- a.  $(D^2 - 5D + 6)y = e^x$
- b.  $(D^2 - 3D + 2)y = \sin 2x$
- c.  $(D^2 + 16)y = \sin x$  (Use the method of variation of parameters)

#### 3. Find the constants $a$ and $b$ so that the surface $ax^2 - byz = (a + 2)x$ will be orthogonal to the surface $4x^2y + z^3 = 4$ at the point $(1, -1, 2)$ .

Show that  $\vec{E} = \frac{\vec{r}}{r^2}$  is irrotational. Find  $\phi$  such that  $\vec{E} = -\nabla\phi$  and such that  $\phi(a) = 0$  where  $a > 0$ .

#### 4. Is there a differentiable vector function $\vec{V}$ such that,

$$\begin{aligned}\nabla \times \vec{V} &= \vec{r} \\ \nabla \times \vec{V} &= 2\hat{i} + \hat{j} + 3\hat{k}\end{aligned}$$

If yes, then find  $\vec{V}$ .

Find the value of  $\nabla^2 \ln r$

#### 5. Verify Green's theorem in the plane for $\oint_C (y - \sin x) dx + \cos x dy$ , where C is the triangle formed by points $(0, 0)$ , $(\frac{\pi}{2}, 0)$ and $(\frac{\pi}{2}, 1)$ .

$$\iiint_V \frac{dV}{r^2} = \iint_S \frac{\vec{r} \cdot \hat{n}}{r^2} dS$$

#### 6. Derive an expression for $\nabla \times \vec{A}$ in orthogonal curvilinear coordinates.

Evaluate  $\iint_S \vec{A} \cdot \hat{n} dS$ , where  $\vec{A} = z\hat{i} + x\hat{j} - 3y^2z\hat{k}$  and S is the surface of the cylinder  $x^2 + y^2 = 16$  included in the first octant between  $z = 0$  to  $z = 5$ .

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